

# Gravitational dipole analyses with partial-sky coverage data

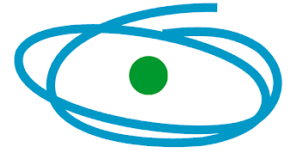
Felipe Avila

Observatório Nacional  
fsavila2@gmail.com

In collaboration with  
A. Bernui & E. de Carvalho



Observatório  
Nacional



C A P E S

XIX Meeting of Physics  
24-26 September 2020 - Lima, Perú

MINISTÉRIO DA  
CIÊNCIA, TECNOLOGIA  
E INOVAÇÕES



PÁTRIA AMADA  
**BRASIL**  
GOVERNO FEDERAL

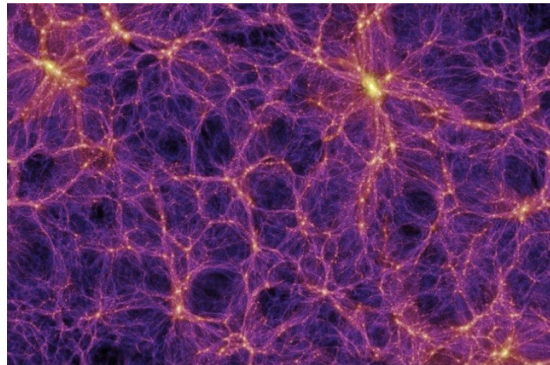
# Outline

- Standard Model of Cosmology
- Cosmic Growth Rate of Structures
- Local Group Dipole
- Methodology
- Results
- Conclusions

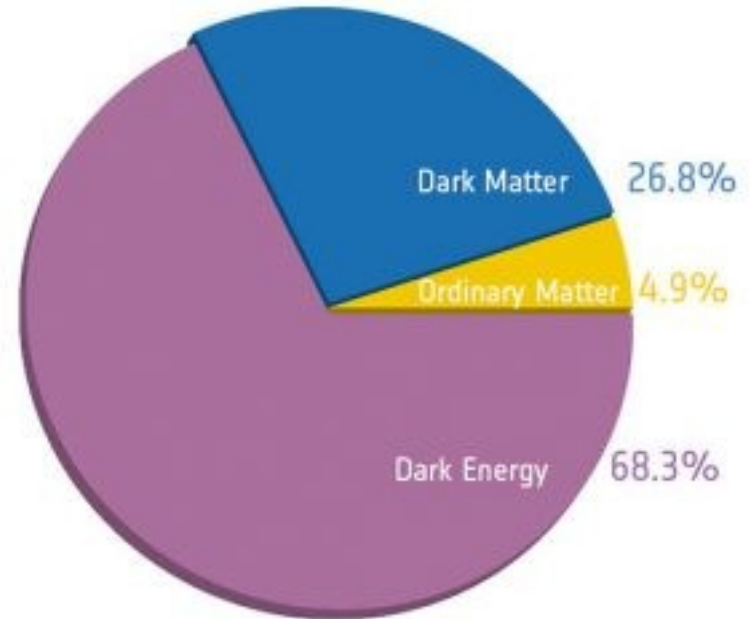
# Standard Model of Cosmology

$$G_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

General Relativity



**Cosmological Principle** – Statistical homogeneity and isotropy at large scale (Avila et al. 2018; arXiv:1806.04541).



We still don't know what dark energy and dark matter are.

# Cosmic Growth Rate

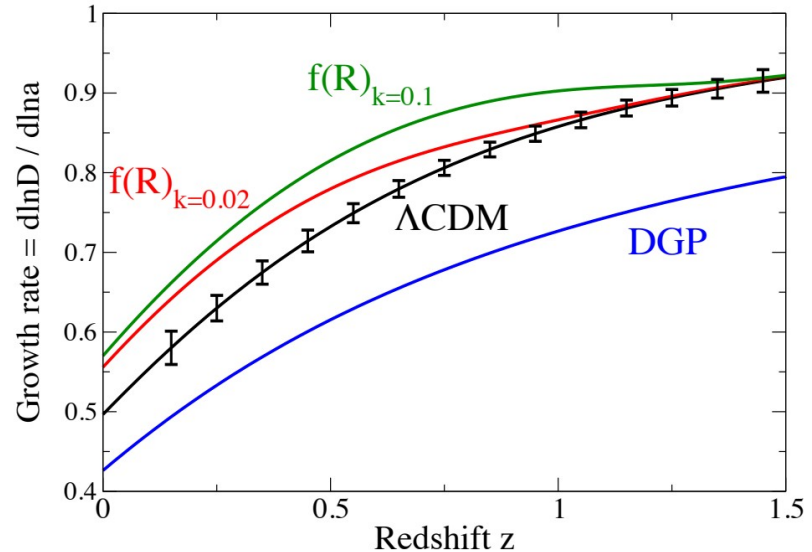
## Linear Perturbation Theory

$$\delta(\mathbf{r}, t) := \frac{\rho(\mathbf{r}, t) - \bar{\rho}(t)}{\bar{\rho}(t)}$$

$$\frac{\partial^2 \delta}{\partial t^2} + \frac{2\dot{a}}{a} \frac{\partial \delta}{\partial t} = 4\pi G \bar{\rho} \delta$$

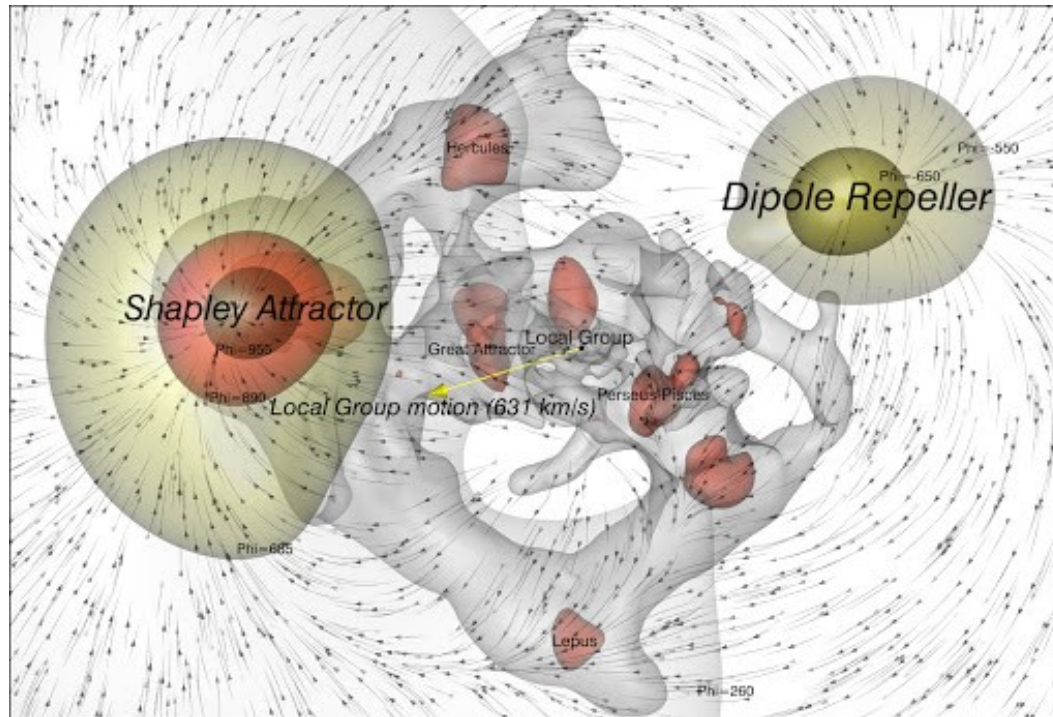
$$\delta(\mathbf{x}, t) = D_+(t) \delta_0(\mathbf{x})$$

$$f(a) := \frac{a}{D_+} \frac{dD_+}{da} = \frac{d \log D_+}{d \log a}$$



# Local Group Dipole

$$\mathbf{u}(\mathbf{x}, t) = \frac{\Omega_m^{0.6}(a)}{4\pi} a H(a) \int d^3y \delta(\mathbf{y}, t) \frac{\mathbf{y} - \mathbf{x}}{|\mathbf{y} - \mathbf{x}|^3} \quad f(a) \approx \Omega_m^\gamma(a)$$



Hoffman et al. (2017)

arXiv:1702.02483

$$u(\mathbf{x}, t) = \frac{\Omega_m^{0.6}(a)}{4\pi} a H(a) \int d^3y \delta(\mathbf{y}, t) \frac{\mathbf{y} - \mathbf{x}}{|\mathbf{y} - \mathbf{x}|^3}$$



$$\mathbf{v}(\mathbf{r}) = \frac{H_0 \beta}{4\pi \langle n \rangle} \int \delta(\mathbf{x}) \frac{\mathbf{x}}{|\mathbf{x}|^3} d\mathbf{r} = \beta \mathbf{D}(\mathbf{r})$$

Volume limited  
survey

$$\mathbf{D} = \frac{H_0}{4\pi \langle n \rangle} \sum \frac{\hat{\mathbf{r}}}{\phi(r) r^2}$$

$$\beta \equiv \Omega_m^{0.6} / b$$

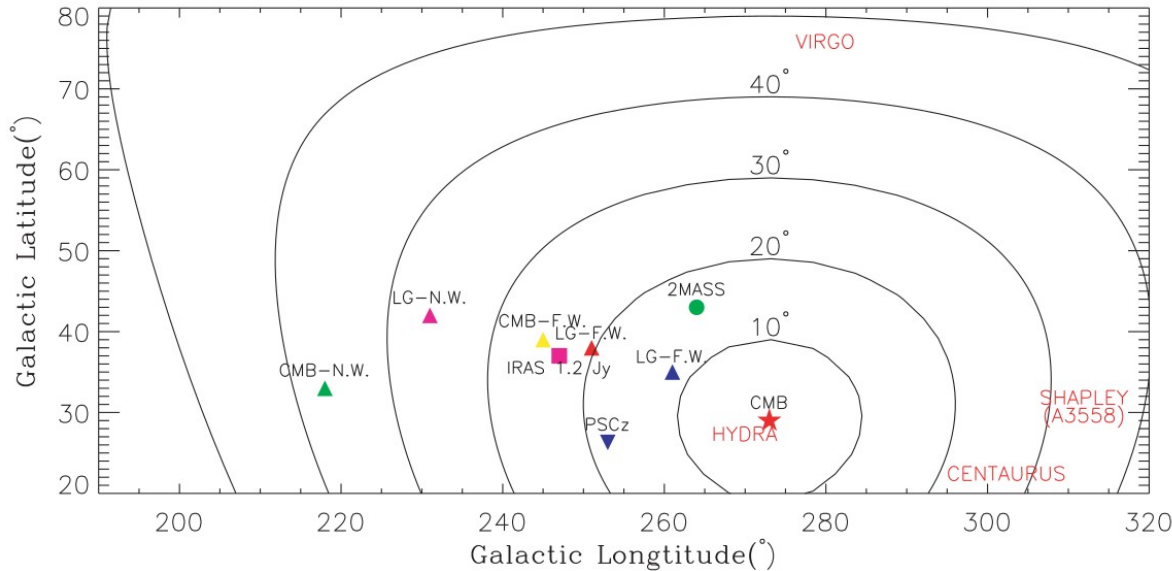
Local Group Velocity

+

Gravitational Dipole



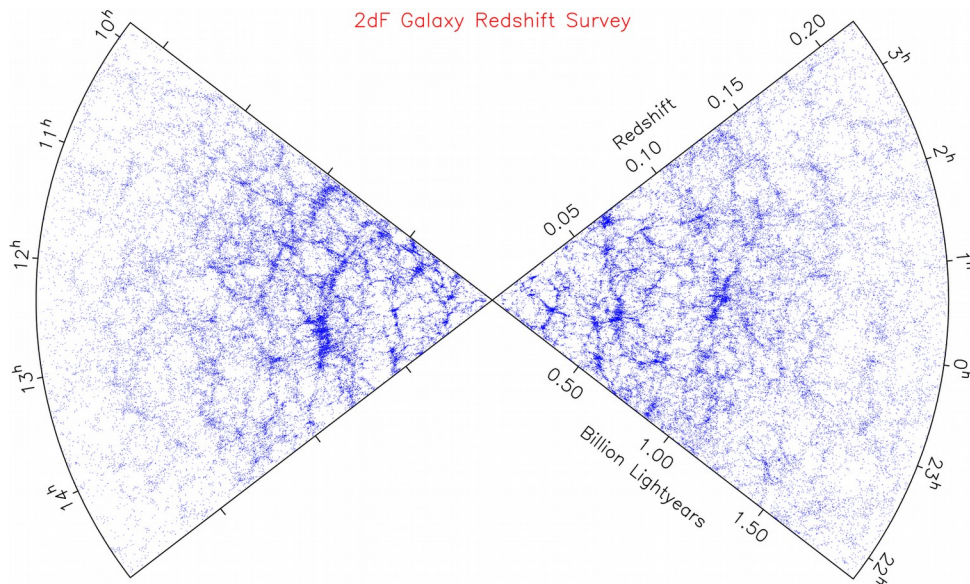
Growth Cosmic Rate



Erdođdu et al. (2006)

# Methodology

- Can the dipole be calculated with partial sky coverage?
  - What is the error involved?



Credit:  
<http://www.2dfgrs.net/>

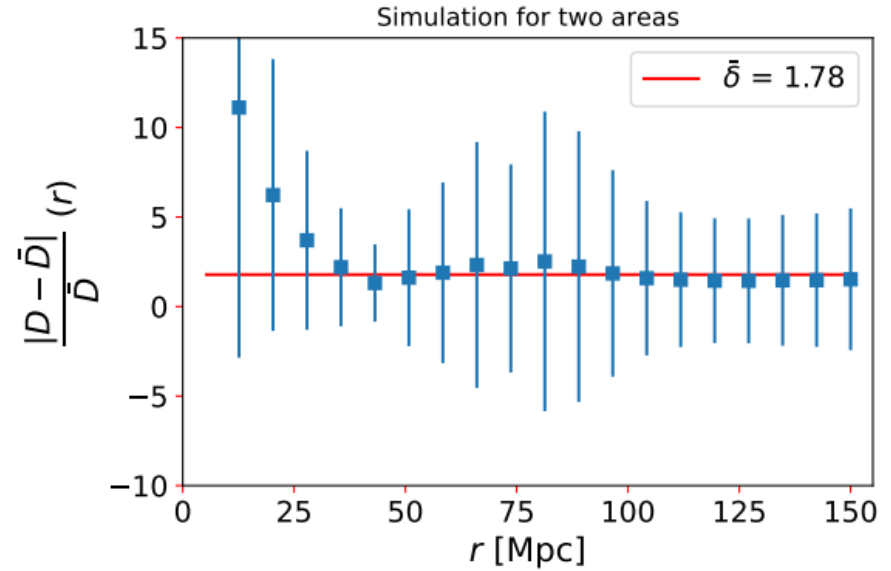
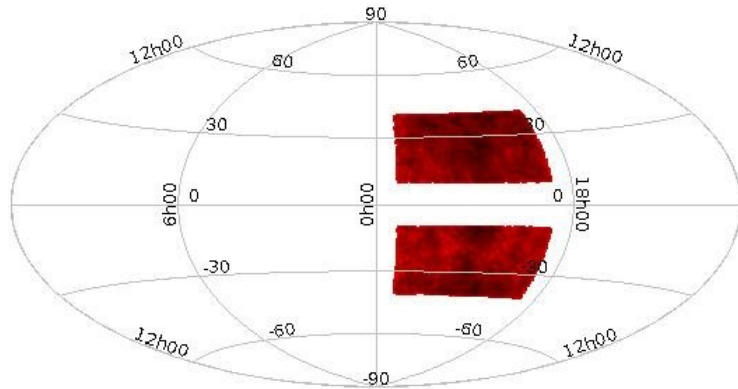
# Lognormal Simulations

- We generated a lognormal catalog with a public code (Agrawal et al., 2017; arXiv:1706.09195).
- We select small pieces of the simulation and relocate them randomly in the sky.
- Angular configuration: 30 deg (declination) x 70 deg (Right Ascension).
- The process is done 2000 times so that all possible combinations can be made.

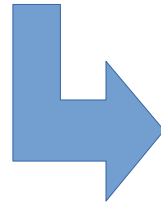
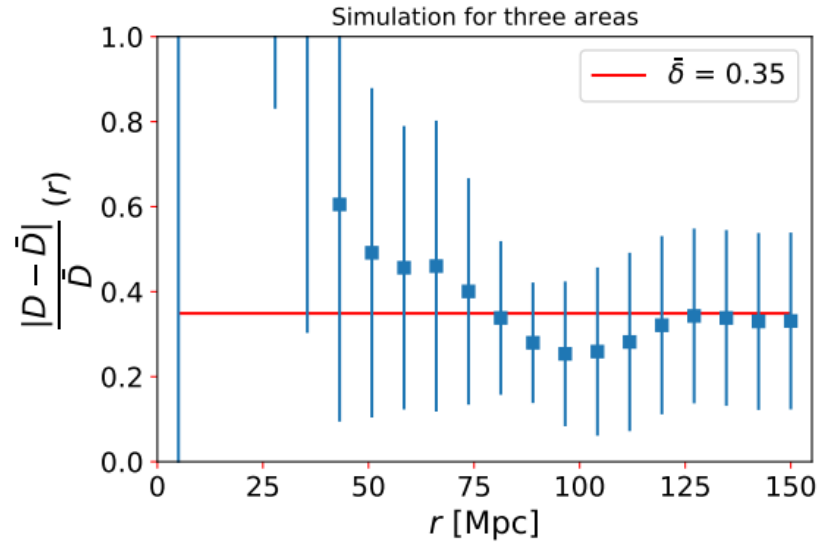
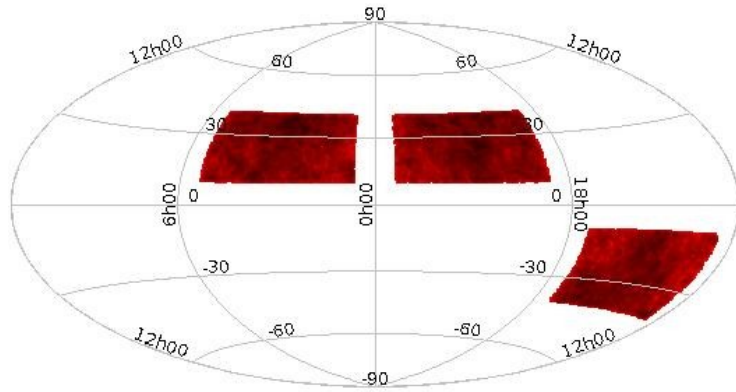


# Results

Configuration 1: 28 possible combinations.

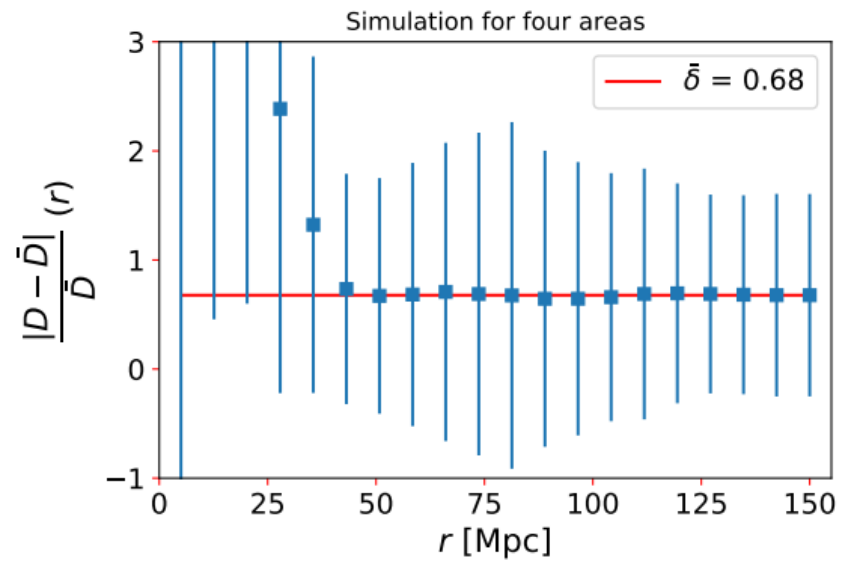
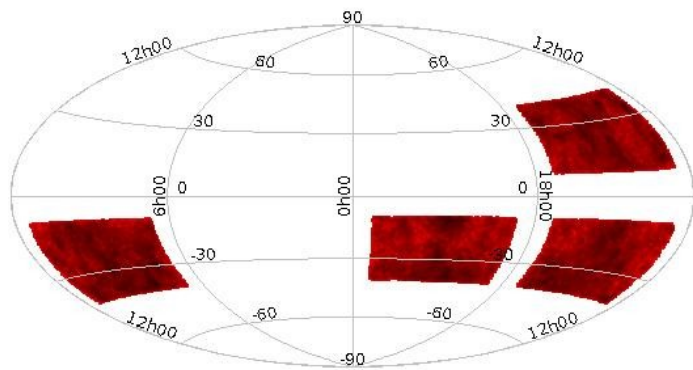


Configuration 2: 56 possible combinations.

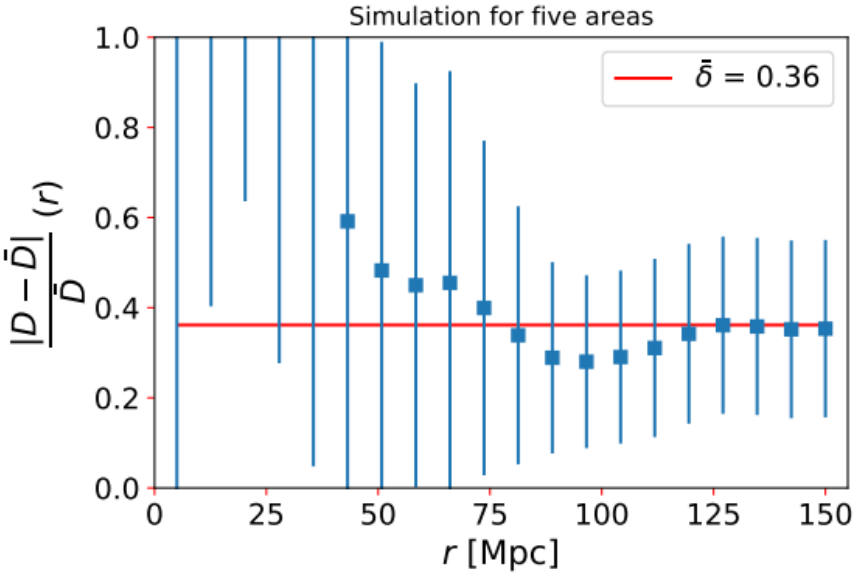
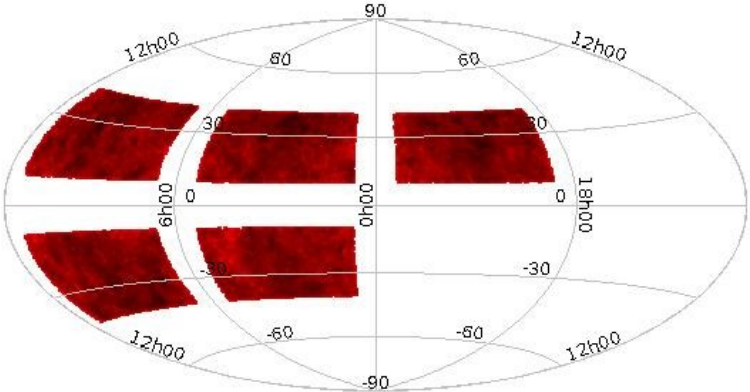


This configuration has the best result, that is, it minimizes the difference in amplitude of the dipole.

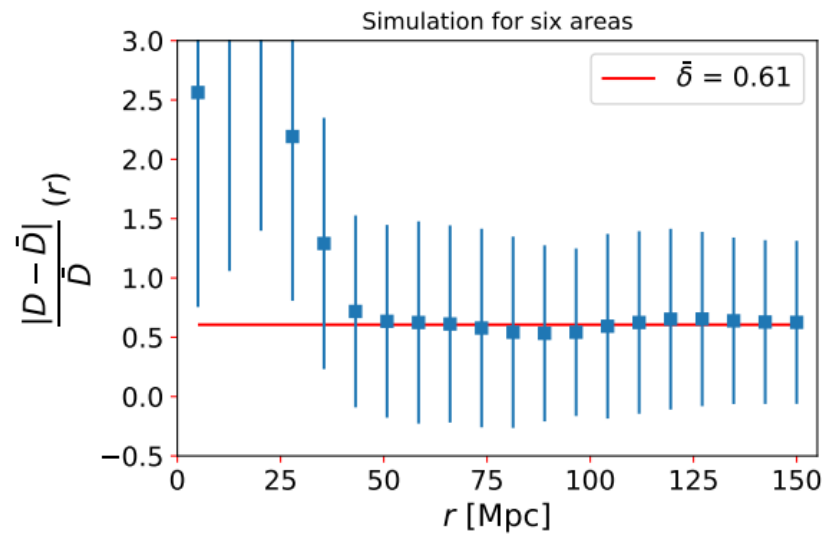
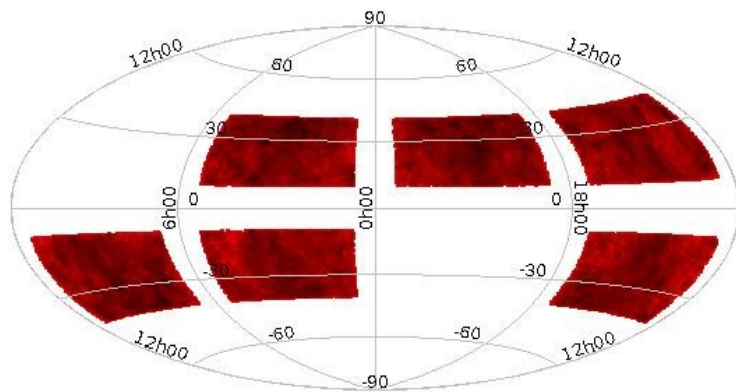
Configuration 3: 70 possible combinations.



Configuration 4: 56 possible combinations.



## Configuration 5: 28 possible combinations.



# Summary and Conclusions

- We want to answer if it is possible to calculate the gravitational dipole with partial sky coverage survey to measure the cosmic growth rate.
- We observe that certain configurations decrease the error in the dipole amplitude.
- The result does not seem to depend on the number of objects.
- For current uncertainty measures in  $\beta$ , we need to lower the dipole amplitude difference to 10%. Therefore it is necessary to look for the configuration that minimizes the error.